

CHAPTER # 3

I This section covers all of the first two pages of this exam. For *each* problem, supply **domain, range, amplitude, period** and **phase shift (including direction word)** and **draw the graph in the areas provided**. Be sure your drawing crosses or approaches the Y-axis. You may do the work for this exam *directly on this* exam paper rather than on the “newsprint” as usual. If you do work on newsprint be sure it is labeled with its problem number. **Indicate significant coordinates** You *may* use decimals for your coordinate responses (however you will probably spend more time using decimals than in not using decimals). Each problem in this section is worth 15 points.

A) $A(x) = 2 \cos\left(\frac{2}{3}x - \frac{\pi}{6}\right) - 1$

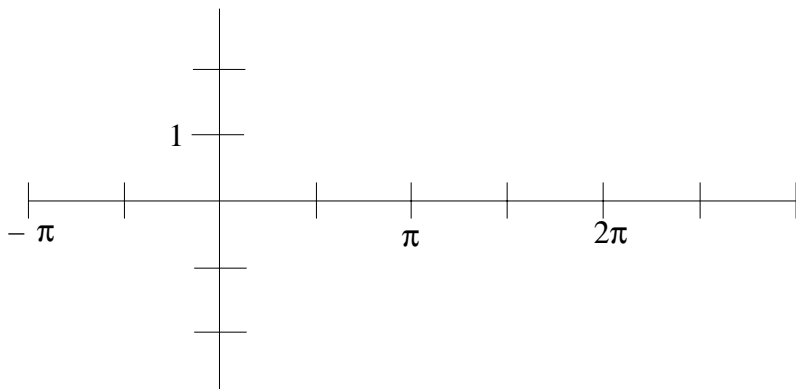
D_A

R_A

Per

Amp

P.S.



B) $B(x) = -\sin\left(\frac{3}{2}x + \frac{\pi}{2}\right)$

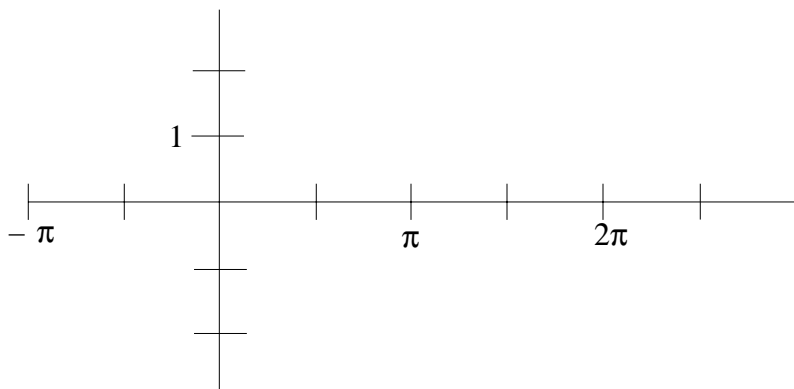
D_B

R_B

Per

Amp

P.S.



C) $C(x) = \csc\left(x - \frac{2\pi}{3}\right) - 1$

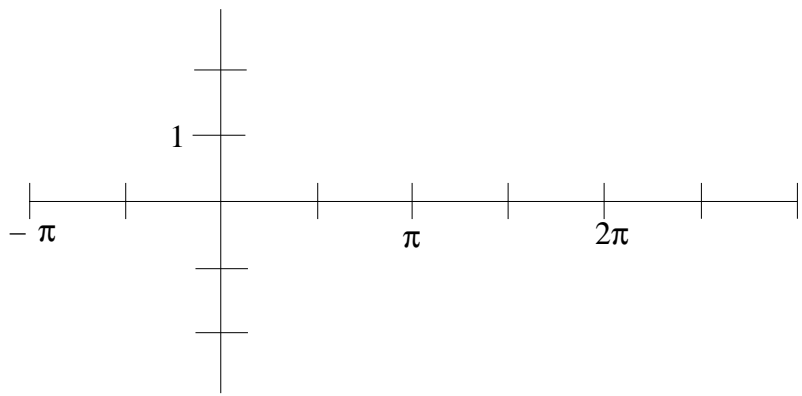
D_C

R_C

Per

Amp

P.S.



D) $D(x) = \tan\frac{4}{3}x$

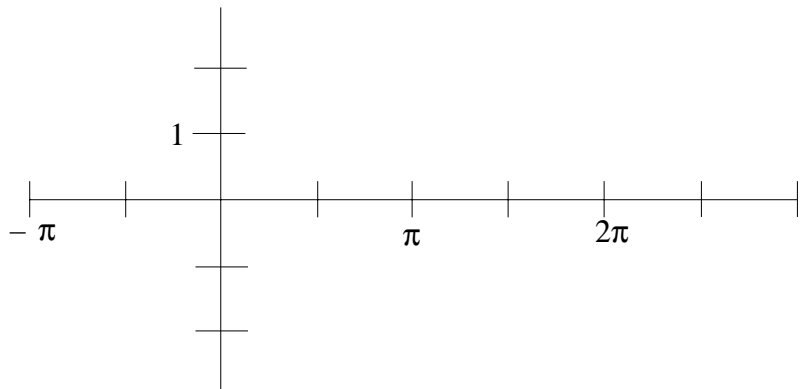
D_D

R_D

Per

Amp

P.S.



E) $E(x) = \sec\frac{2}{3}x$

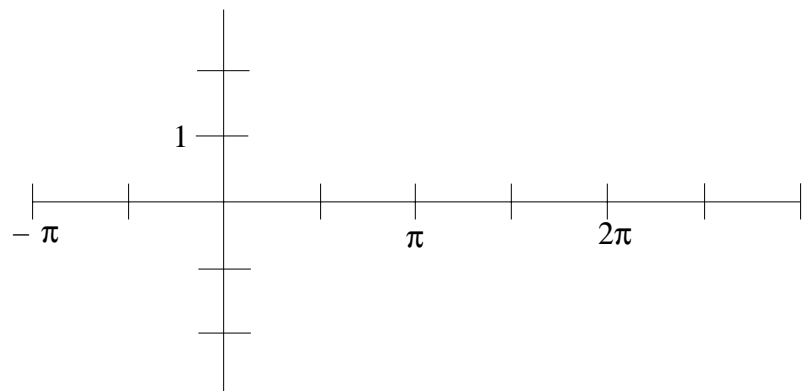
D_E

R_E

Per

Amp

P.S.



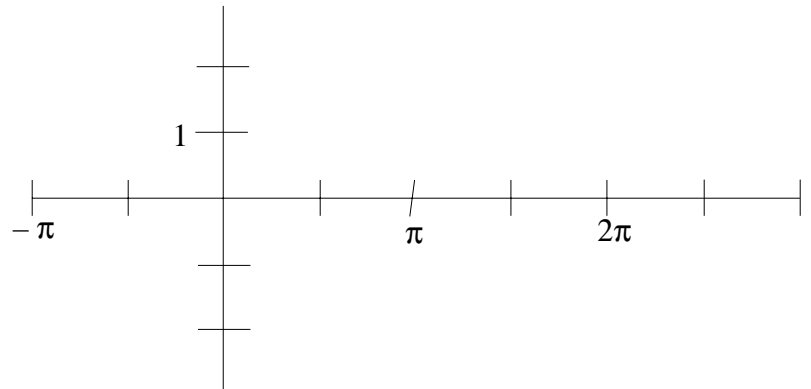
II

Draw a sketch of $\tan x$ and $\cot x$ on the supplied axis.

(15 pts total)

Describe what must be done to $\tan x$ to make it coincide with $\cot x$.

Prove that your changes would have the desired effect.

**III**

Given P_1 starts at $\left(\frac{-1}{2}, \frac{\sqrt{3}}{2}\right)$ with $\omega_1 = \frac{\pi}{4}$ and P_2 starts at $\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$ with $\omega_2 = \frac{\pi}{3}$

(10 pts tot)

A) Find t when the two points first coincide.

B) Confirm that P_1 and P_2 do, in fact, have the same coordinates at the t found in part A.

EXTRA CREDIT ----- **5 pts** -----

As you know, to prove a function has period “ a ” you must show that $f(x + a) = f(x)$.

Given $f(x) = \cos 2x \sin x + \sin 2x \cos x$. Prove $f(x)$ has period $\frac{2\pi}{3}$.